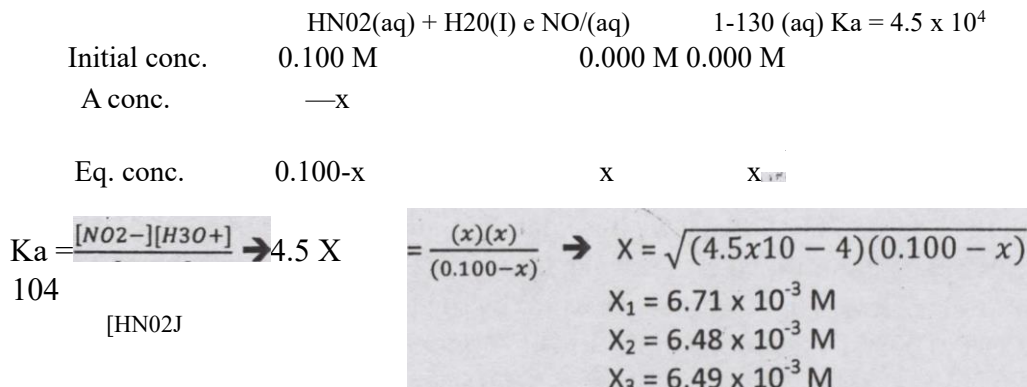


Problem-Solving: Calculating the pH for a Titration Problem.

4

Suppose one begins with 50.0-mL a 0.100 M solution of nitrous acid. The $K_a = 4.5 \times 10^{-4}$
 What is the pH after (a) 0.0 mL of 0.125 M NaOH is added? (b) After 10.0 mL? (c) After 17.0 mL? (d) After 20.0 mL? (e) After 39.0 mL? (f) After 40.0 mL? (g) After 45.0 mL?

(a) Adding 0.0 mL of 0.125 M NaOH: Calculate the pH using the ICE solution.



$$X = 0.100 - 1 = 6.5 \times 10^{-3} \text{ M} \quad \text{pH} = -\log [\text{H}_3\text{O}^+] = -\log 6.5 \times 10^{-3} \text{ M} = \underline{2.19}$$

(b) After initial calculation and before the equivalence point, the system has a buffer.

Initial number of moles of HN02: $0.100 \text{ M} (0.050 \text{ L}) = 0.0050 \text{ moles acid}$

Adding 10.0 of 0.125 M NaOH: $0.125 \text{ M} (0.010 \text{ L}) = 0.00125 \text{ mol base}$

$$\text{pH} = \text{p}K_a + \log \frac{(\text{c.base})}{(\text{0} + 0.00125)} = 3.35 + \log \frac{0.00125}{(0.0050 - 0.00125)} = 3.35 + \log \frac{0.00125}{0.00375} = 3.35 + (-0.48) = \underline{2.87}$$

(c) After adding 17.0 mL of 0.125 M NaOH: $0.125 \text{ M} (0.017 \text{ L}) = 0.002125 \text{ moles base}$

$$\text{pH} = 3.35 + \log \frac{(0.002125)}{(0.0050 - 0.002125)} = 3.35 + \log \frac{0.002125}{0.002875} = 3.35 + 0.13 = \underline{3.22}$$

(d) After adding 20.0 mL of 0.125 M NaOH: $0.125 \text{ M} (0.020 \text{ L}) = 0.0025 \text{ moles base}$

$$\text{pH} = 3.35 + \log \frac{(0.0025)}{(0.0050-0.0025)} = 3.35 + \log \frac{0.0025}{0.0025} = 3.35 - 0.00 = \underline{3.35}$$

We are halfway to the equivalence point, so $\text{pH} = \text{pKa}$

(e) After adding 39.0 mL of 0.125 M NaOH: $0.125 \text{ M} (0.0390 \text{ L}) = 0.004875$ moles base

$$\text{pH} = 3.35 + \log \frac{(0.004875)}{(0.0050-0.004875)} = 3.35 + \log \frac{0.004875}{0.000125} = 3.35 + 1.59 = \underline{4.94}$$

(f) After adding 40.0 mL of 0.125 M NaOH: $0.125 \text{ M} (0.0400 \text{ L}) = 0.0050$ moles base
Moles of acid = moles of NaOH added. We have reached the equivalence point!

Do an ICE procedure using the K_b of the conj. base of HNO_2 . Namely NO_2^-

	(aq)	+ H ₂ O(l)	⇌	HNO ₂ (aq)	+ OH ⁻ (aq)	$K_b = \frac{K_a}{K_w} = 2.2 \times 10^{-11}$
Initial conc.	$\frac{0.0050 \text{ mol}}{0.090 \text{ L}}$			0.000 M	0.000 M	
conc.	-x				x	
Eq. conc.	$0.0556 - x$			x	x	

$$K_b = \frac{[\text{HNO}_2][\text{OH}^-]}{[\text{NO}_2^-]} \rightarrow 2.2 \times 10^{-11} = \frac{(x)(x)}{(0.0556-x)} \rightarrow x = \sqrt{(2.2 \times 10^{-11})(0.0556-x)}$$

$$x_1 = 1.11 \times 10^{-6} \text{ M}$$

$$x_2 = 1.11 \times 10^{-6} \text{ M}$$

$$x = [\text{OH}^-] = 1.1 \times 10^{-6} \text{ M} \quad \text{pOH} = -\log [\text{OH}^-] = 5.96 \quad \text{pH} = 14.00 - 5.96 = \underline{8.04}$$

(g) With the addition of 45.0 mL, we have passed the equivalence point and the only species of any importance is the strong base, NaOH. Remember, at the eq. point, no NaOH exists. It was neutralized into water by the hydronium ion. Soooooo.....

$0.125 \text{ M} (0.005 \text{ L}) = 0.000625$ moles of OW / $0.095 \text{ L} = 0.00658 \text{ M} = [\text{OH}^-]$

Excess NaOH after eq. pt. total volume

POH = 2.18, pH = 11.82

YOU ARE FINISHED!!!